

ASME B31J-2023
(Revision of ASME B31J-2017)

Stress Intensification Factors (*i*-Factors), Flexibility Factors (*k*-Factors), and Their Determination for Metallic Piping Components

ASME Code for Pressure Piping, B31

AN AMERICAN NATIONAL STANDARD



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CONTENTS

Foreword	v
Committee Roster	vi
Correspondence With the B31 Committee	vii
Introduction	viii
Summary of Changes	x
1 General	1
2 Definitions	1
3 Contents Of Standard	1
4 Reference	1
Nonmandatory Appendices	
A Stress Intensification Factor (SIF) Test Procedure	18
B Test Method for Determining Branch Connection Flexibility Factors	27
C Use Of Branch Connection Flexibility Factors in Piping System Analysis	36
D Sustained Load Test Procedure	40
Figures	
1-1 Orientations for Sketches 2.1 Through 2.6 of Table 1-1	14
1-2 Orientations for Bends	15
1-3 Branch Dimensions	15
1-4 Flexibility and Stress Intensification Factors for Bends and Miters	16
1-5 Flanged End Corrections for Bends and Miters	16
1-6 Flexibility Element Locations	17
1-7 Fillet Weld Contours	17
A-1.1-1 Representative Cantilever Test Arrangements	18
A-1.3-1 Displacement and Force or Moment Recorded During Loading and Unloading of a Test Specimen in Both Positive and Negative Directions, With Linear Displacement	20
B-1-1 Branch Connection Specimen	27
B-1-2 Multiple <i>k</i> -Factor Tests on Single Assembled Position	28
B-2-1 Example Flexibility Factor Branch Load Assembly Orientation	29
B-4.4-1 Detailed Beam Model for Through-Branch <i>k</i> -Factor Test	31
B-4.4-2 Beam Model	32
B-4.6-1 Load-Displacement Diagram	33
B-6-1 Unreinforced Branch Connection With (Left) and Without Ovalization Restraint Plates in Place	34
C-2-1 Rotational Stiffness Location Between Two Nodes	36
C-2-2 Branch Connection In-Plane Direction	37
C-2-3 Branch Connection Flexibilities Used on Branch Side Only	38
C-2-4 Branch Connection Flexibilities Used on Run Side Only	38

C-2-5	Branch and Run Flexibilities Used Together (in Series)	38
C-2-6	Rotational Flexibility Definitions	39
C-2-7	Branch and Run SIF and k -Factor Intersection Orientations	39
D-1-1	Standard Sustained Load Setup	40
D-1-2	Bend Sustained Load Setup	41
D-2-1	Load-Displacement Diagram Illustrating Typical Pressure-Sensitive, Not Pressurized, and Not-Pressure-Sensitive Load-Deflection Behavior	42
D-3-1	Load-Displacement Diagram at $d_s = 2d_e$ Limit	44

Tables

1-1	Flexibility and Stress Intensification Factors	2
1-2	Moment-Rotation Relationships for Sketches 2.1 Through 2.6 of Table 1-1	14
1-3	Flanged End Correction Coefficients for Sketches 2.1 Through 2.6 of Table 1-1	14
A-2.4-1	Stress Intensification Increase Factor	21
B-1-1	Load-Deflection Pairs for Single Assembled Orientation Shown in Figure B-1-2	28
D-8.1-1	Distance and Precaution for Pressurized Twice Elastic Slope Test	49
D-8.1-2	Inadvertent Air Volumes in Test Specimens	50

FOREWORD

In 1990 The American Society of Mechanical Engineers (ASME) B31 Code for Pressure Piping Technical Committee on Mechanical Design (MDC) recognized a need for a standard method to develop stress intensification factors (SIFs or *i*-factors) for ASME piping components and joints. At the time, the B31 Code books provided SIFs for various standard fittings and joints but did not provide guidance on how to conduct further research on existing SIFs or how to establish SIFs for nonstandard and other standard fittings or joints.

In 2001 the MDC realized that SIFs and *k*-factors in the various ASME B31 Code books were not consistent or up to date. ASME initiated a research project completed by the MDC that incorporated recent research and current manufacturing practices into the SIF and *k*-factor test procedures. This resulted in a consistent and up-to-date table of SIFs and *k*-factors for metallic piping components.

ASME B31J provides a standard approach for the development of SIFs, *k*-factors, and sustained stress multipliers for piping components and joints of all types, including standard, nonstandard, and proprietary fittings.

Sustained stress multipliers are used to multiply the nominal bending stress due to sustained loading and reflect the collapse capacity of the metallic piping component or joint. Multipliers of the nominal bending stress due to sustained loads currently exist explicitly in some, but not all, B31 books. Where more accurate sustained stresses are needed but an equation for the sustained stress is not given in the B31 Code book, nominal stresses due to sustained moments computed using the section modulus of the matching pipe should be multiplied by the appropriate sustained stress multiplier. Where the sustained stress is needed and an equation for the sustained stress is given in the Code book as a function of the SIF and provided in lieu of more applicable data, the sustained stress multipliers developed using the method in this Standard may be substituted as more applicable data and used with the nominal stress computed using the section modulus of the matching pipe.

The most applicable currently available stress intensification and flexibility factors compiled from test and analysis data for standard commercially available metallic components are included in [Table 1-1](#) and should be used with the section modulus of the matching pipe (not an “effective” section modulus). [Nonmandatory Appendix A](#) provides the standard method to develop stress intensification factors. [Nonmandatory Appendix B](#) provides the standard method to develop branch connection flexibility factors. [Nonmandatory Appendix C](#) demonstrates how the new branch connection *k*-factors should be used in the elastic analysis of piping systems, and [Nonmandatory Appendix D](#) provides a standard method to develop sustained stress factors. A procedure to develop *k*-factors for bends, elbows, and straight pipe is available in Rodabaugh and Wais.¹

This Standard has been reviewed by individuals and appropriate subcommittees of the Boiler and Pressure Vessel Code, B31, and B16 Committees. Comments resulting from the review have been considered and responded to, with revisions made to the Standard, as appropriate. ASME B31J-2023 was approved as an American National Standard by the American National Standards Institute on July 17, 2023.

¹Rodabaugh, E. C., and Wais, E. A. (2001). Report 1: Standardized Method for Developing Flexibility Factors for Piping Components (WRC Bulletin 463). Welding Research Council.

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Code for Pressure Piping

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Revisions and Errata. The committee processes revisions to this Standard on a continuous basis to incorporate changes that appear necessary or desirable as demonstrated by the experience gained from the application of the Standard. Approved revisions will be published in the next edition of the Standard.

In addition, the committee may post errata on the committee web page. Errata become effective on the date posted. Users can register on the committee web page to receive e-mail notifications of posted errata.

This Standard is always open for comment, and the committee welcomes proposals for revisions. Such proposals should be as specific as possible, citing the paragraph number, the proposed wording, and a detailed description of the reasons for the proposal, including any pertinent background information and supporting documentation.

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Committee Meetings. The B31 Standards Committee regularly holds meetings that are open to the public. Persons wishing to attend any meeting should contact the secretary of the committee. Information on future committee meetings can be found on the committee web page at <https://go.asme.org/B31committee>.

INTRODUCTION

The ASME B31 Code for Pressure Piping consists of a number of individually published Sections and Standards, each an American National Standard, under the direction of the ASME B31 Code for Pressure Piping Committee.

Rules for each Section reflect the kinds of piping installations considered during its development, as follows:

B31.1	Power Piping: piping typically found in electric generating stations, in industrial and institutional plants, in geothermal and solar power applications, and in central and district heating and cooling systems
B31.3	Process Piping: piping typically found in petroleum refineries and in chemical, pharmaceutical, textile, paper, semiconductor, cryogenic, and related processing plants and terminals
B31.4	Pipeline Transportation Systems for Liquid Hydrocarbons and Other Liquids: piping that transports products that are predominately liquid between plants and terminals, and within terminals and pumping, regulating, and metering stations
B31.5	Refrigeration Piping: piping for refrigerants and secondary coolants
B31.8	Gas Transportation and Distribution Piping Systems: piping that transports products that are predominately gas between sources and terminals, including compressor, regulating, and metering stations and gas gathering pipelines
B31.9	Building Services Piping: piping typically found in industrial, institutional, commercial, and public buildings and multiunit residences that do not require the range of sizes, pressures, and temperatures covered by B31.1
B31.12	Hydrogen Piping and Pipelines: piping in gaseous and liquid hydrogen service and pipelines for gaseous hydrogen service

Rules for each Standard provide guidance for a specific task found in one or more B31 Section publications, as follows:

B31E	B31E, Seismic Design and Retrofit of Above-Ground Piping Systems, establishes a method for the seismic design of above-ground metallic piping systems in the scope of the ASME B31 Code for Pressure Piping.
B31G	Remaining Strength of Corroded Pipelines, provides a simplified procedure to determine the effect of wall loss due to corrosion or corrosion-like defects on the pressure integrity in pipeline systems.
B31H	Standard Method to Establish Maximum Allowable Design Pressure for Piping Components, provides a standardized method to perform a proof (burst) test for piping components and joints (under development).
B31J	Stress Intensification Factors (<i>i</i> -Factors), Flexibility Factors (<i>k</i> -Factors), and Their Determination for Metallic Piping Components, provides a standardized method to develop the stress intensification factors (<i>i</i> -factors), flexibility factors (<i>k</i> -factors), and sustained stress factors used in ASME B31 piping analysis.
B31T	Standard Toughness Requirements for Piping, provides requirements for evaluating the suitability of materials used in piping systems for piping that may be subject to brittle failure due to low-temperature service conditions.

This B31J Standard provides stress intensification factors (*i*-factors) and flexibility factors (*k*-factors), with procedures for their determination for metallic piping components and joints. Stress intensification and flexibility factor equations for common piping components are provided in [Table 1-1](#). The sustained load test procedure can be used to determine more applicable nominal stress multipliers for use in sustained and occasional ASME B31 analyses. Hereafter, in this Introduction and throughout the text of this B31 Standard, where the word *Standard* is used without further identification, it means this B31J Standard.

This Standard sets forth stress intensification factors, flexibility factors, and engineering procedures deemed appropriate for the safe determination of the fatigue and sustained load capacity of metallic piping components or joints in typical services. The procedure cannot foresee all geometries and services possible, and the use of competent engineering

judgment may be necessary to extend the procedure to cover unusual geometries and service conditions or to ensure a safe testing environment.

The ASME B31 Committee is organized and operates under procedures of The American Society of Mechanical Engineers, which have been accredited by the American National Standards Institute. The Committee is continuing and keeps all Code Sections and Standards current with new developments in methods, materials, construction, and industrial practice. New editions are published or reaffirmed at intervals of 3 to 5 years.

This edition of the B31J Standard is not intended to be retroactive. Unless agreement is specifically made between contracting parties to use another edition, or a regulatory body having jurisdiction imposes the use of another edition, the latest edition issued at least 6 months prior to the original contract date for the piping installation activity in which a component or joint qualified by this Standard is to be used shall be the governing document for the determination of SIFs and k -factors. Users of this Standard are cautioned against making use of Standard revisions without assurance that they are acceptable to the proper authorities in the jurisdiction where the piping component is to be installed.

ASME B31J-2023

SUMMARY OF CHANGES

Following approval by the ASME B31 Committee and ASME, and after public review, ASME B31J-2023 was approved by the American National Standards Institute on July 17, 2023.

ASME B31J-2023 includes the following changes identified by a margin note, **(23)**.

<i>Page</i>	<i>Location</i>	<i>Change</i>
viii	Introduction	First sentence of last paragraph editorially revised
1	1	Reference to ASME BPVC, Section III updated
2	Table 1-1	(1) Equations for sketch 1.1, SIF in plane and out of plane, revised (2) Equations for sketches 2.1, 2.4, and 2.6, run SIF in plane, i_{ir} , revised (3) Equations for sketch 2.3, run SIF in plane, i_{ir} , and branch SIF out of plane, i_{ob} , revised (4) In General Note (a), variable h added and variable I revised to i (5) General Note (d) and Notes (6), (7)(f), and (9) revised, and General Note (e) added
1	3	(1) Title revised (2) Subparagraph (a) editorially revised
18	Nonmandatory Appendix A	References reformatted throughout
19	A-1.2	Last sentence of second paragraph editorially revised
19	A-1.3(a)	Last sentence editorially revised
20	A-2.3	Definition of variable S in eq. (A-3) revised
23	A-5.1	(1) In last paragraph, cross-references updated (2) Subparagraph (c) editorially revised
27	Nonmandatory Appendix B	References reformatted throughout
27	B-1(c)	Editorially revised
27	B-1.1	Third sentence of second paragraph editorially revised
30	B-3	For variables S_y and S_{yp} , “Record” revised to “Report”
32	B-4.6(g)	Last sentence deleted
36	C-1	Definition of variable r corrected by errata
40	Nonmandatory Appendix D	References reformatted throughout
41	D-1.2(d)	Last sentence editorially revised
41	D-2	Definition of <i>test pressure</i> editorially revised

STRESS INTENSIFICATION FACTORS (*i*-FACTORS), FLEXIBILITY FACTORS (*k*-FACTORS), AND THEIR DETERMINATION FOR METALLIC PIPING COMPONENTS

(23) 1 GENERAL

The ASME B31 Code for Pressure Piping and the ASME Boiler and Pressure Vessel Code (BPVC), Section III, Subsection NCD piping rules require the use of stress intensification factors (SIFs or *i*-factors) and flexibility factors (*k*-factors) when checking the adequacy of components and joints (welded and nonwelded) in piping subject to various loads, including cyclic loads, that may produce fatigue failures. As used herein, where the word “Code” is used without specific identification, it means the code that incorporates or references this Standard. Experimental methods to determine SIFs, flexibility factors, and sustained load factors are provided in the Nonmandatory Appendices. Compiled stress intensification and flexibility factor equations for common piping components are included in [Table 1-1](#); see also [Tables 1-2](#) and [1-3](#) and [Figures 1-1](#) through [1-7](#).

2 DEFINITIONS

flexibility factor: for branch connections and reducers, a ratio that defines the rotation of one end of a zero- or negligible-length element with respect to the opposite end of the same element when equal and opposite moments are applied at each end; for bends, a factor based on an effective length of matching pipe that increases the element flexibility to simulate the effect of bend ovalization that applies over the entire arc length of the bend.

i-factor: the same as the stress intensification factor.

k-factor: the same as the flexibility factor.

pipe stress analyst: the individual responsible for the accuracy of *i*-factors, *k*-factors, and sustained load factors used in the analysis of the piping system.

piping components: mechanical elements suitable for joining or assembly into pressure-tight, fluid-containing piping systems. Components include pipe, tubing, fittings, flanges, gaskets, bolting, valves, and devices such as expansion joints, flexible joints, pressure hoses, traps, strainers, in-line portions of instruments, and separators.

stress intensification factor (SIF): a piping component fatigue strength factor. It is the ratio of the elastically calculated nominal stress in matching pipe that causes

a through-wall crack to appear in a given number of cycles in a straight pipe butt weld to the elastically calculated nominal stress in the matching pipe used with the component that produces a through-wall crack in the same number of cycles in the component or attached pipe.

verified numerical analysis: typically, a finite element analysis of a particular piping system component whose results have been verified against existing test data.

3 CONTENTS OF STANDARD

(23)

(a) There are several different tests the manufacturer or user of a metallic piping component may conduct to demonstrate the component's Code adequacy. These tests include burst tests, load-deflection tests (*k*-factor tests), SIF tests (*i*-factor tests), and sustained load tests. Multiple tests may be performed on the same specimen. For example, SIF tests can follow multiple *k*-factor tests, and sustained load tests can follow SIF tests when the specimen has been suitably repaired.

(b) Typical tests conducted as part of a piping component evaluation include, but are not limited to, the following:

- (1) burst test
- (2) SIF test (in accordance with [Nonmandatory Appendix A](#))
- (3) *k*-factor test (in accordance with [Nonmandatory Appendix B](#))
- (4) sustained load test (in accordance with [Nonmandatory Appendix D](#))

Procedures for the tests in (2) through (4) are described in the nonmandatory appendices in this Standard.

(c) Stress intensification and flexibility factors for metallic piping components are included in [Table 1-1](#) and were developed using the test procedures in this Standard and numerical methods.

4 REFERENCE

Rodabaugh, E. C. (1994). Part 1: Standardized Method for Developing Stress Intensification Factors for Piping Components (WRC Bulletin 392). Welding Research Council.